Exercises for Computability and Complexity, Spring 2018, Sheet 7

Please return your solutions in the Thursday lecture on April 5

Exercise 1 (easy). Show that **and true true** $=$ **true**. You may use **if true** $s\ t \rightarrow* s$ and **and** $\equiv$ $\lambda pq.$ **if** $p\ q$ **false.**

Exercise 2 (medium – many simple solutions exist, but you have to "see" them…) Define three λ-terms **a**, **b**, **c** and another λ-term **L** such that **Laa** $=$ **Lbb** $=$ **Lcc** $=$ **Lba** $=$ **Lca** $=$ **Lcb** $=$ **false**, and **Lab** $=$ **Lac** $=$ **Lbc** $=$ **true**. (You may think of **L** as a "properly less than" ordering of **a**, **b**, **c**). Hint: use some of the λ-terms from the lecture notes (Booleans, list operators) in the makeup of **a**, **b**, **c** and **L**.